



Determination of the patch loading resistance of girders with corrugated webs using nonlinear finite element analysis

László Dunai

Professor

BME Dept.of Structural Engineering

Balázs Kövesdi

PhD Student

BME Dept. of Structural Engineering



Contents

- **Experimental investigations**
 - Patch loading experiments on girders with corrugated webs

- **Numerical investigations**
 - FEM model development
 - Comparison of numerical simulations and test results

- **FEM based desing method**
 - Investigations for the equivalent geometric imperfections
 - Imperfection shapes
 - Imperfection scaling factor

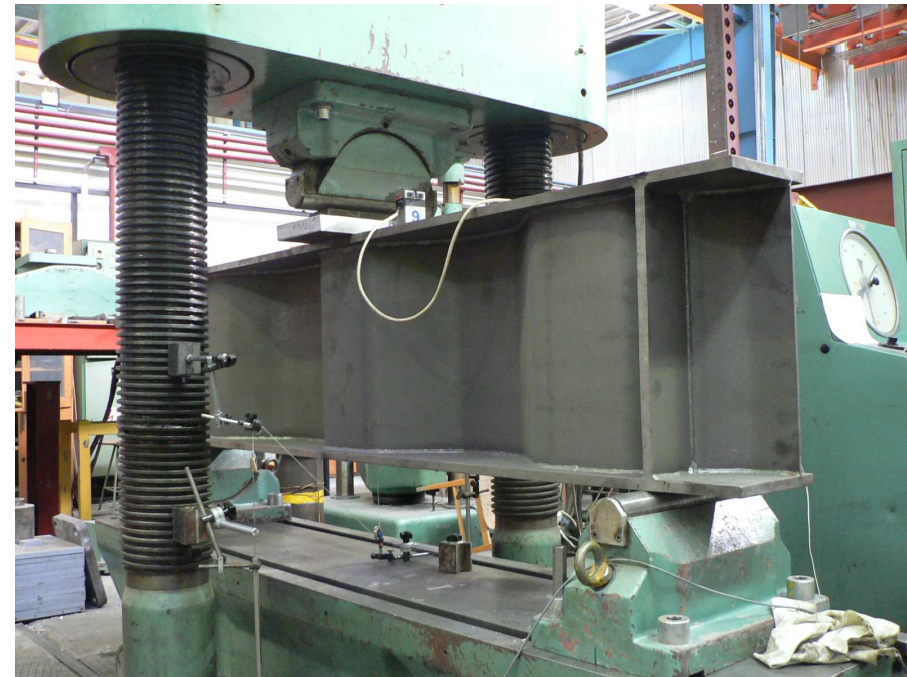
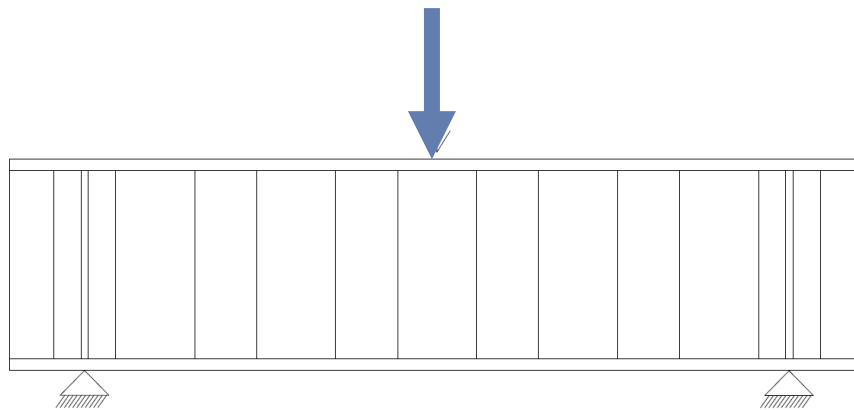
- **Conclusions**

Patch loading tests

Experimental program 12 test specimens

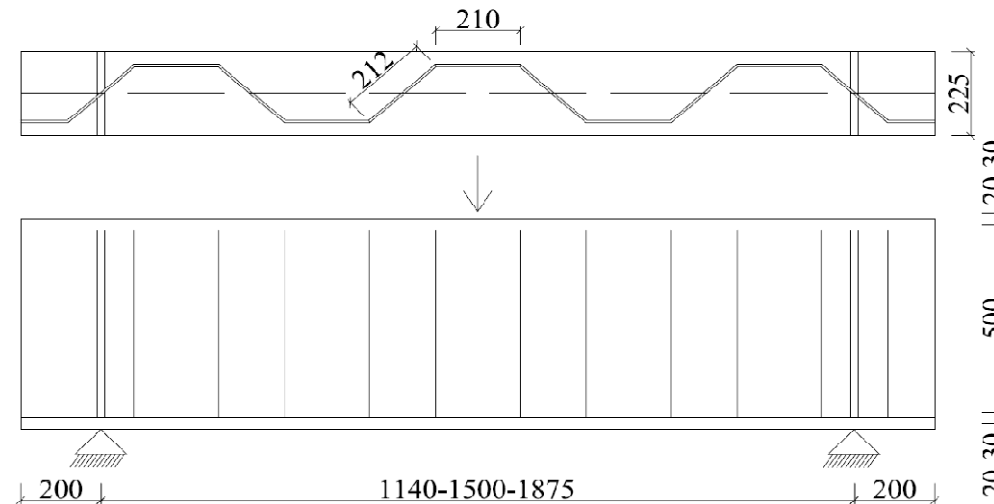
- Aims of the tests**
1. Determination of the patch loading resistance for different geometrical arrangement.
 2. Verification of the developed design method.
 3. Development of FEM based design method.

Test arrangement



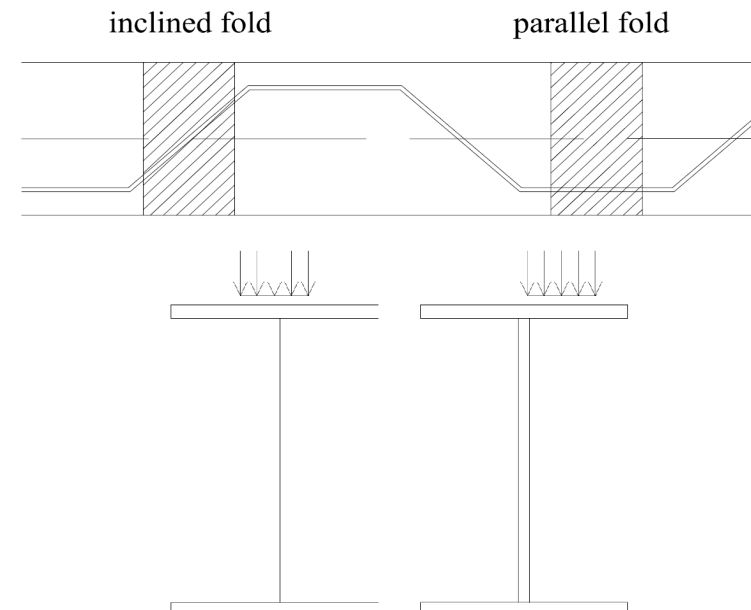
Patch loading tests

Test specimens


 $h_w=500\text{mm}$
 $t_w=6\text{mm}$
 $b_f=225\text{mm}$
 $t_f=20\text{mm}; 30\text{mm}$
 $\alpha=39^\circ$
 $a_1=210\text{mm}$
 $a_2=212\text{mm}$

Analysed parameters

1. loaded fold (parallel, inclined, corner area)
2. loading length (90mm, 200mm, 380 mm)
3. span (1140mm, 1500mm, 1875 mm)
4. flange thickness (20mm, 30 mm)
5. loading eccentricity in transverse direction



Patch loading tests

Failure modes

- loading length
- loaded fold

loaded fold: parallel fold
loading length: 90mm



loaded fold: parallel fold
loading length: 200mm





FEM based design method

Research strategy

1. FE model development for all test specimens

2. Experimental patch loading resistance \longleftrightarrow numerical resistance

3. Experimental failure mode \longleftrightarrow numerical failure mode

4. Experimental load-displacement diagram \longleftrightarrow numerical analysis

5. Verification of the numerical model

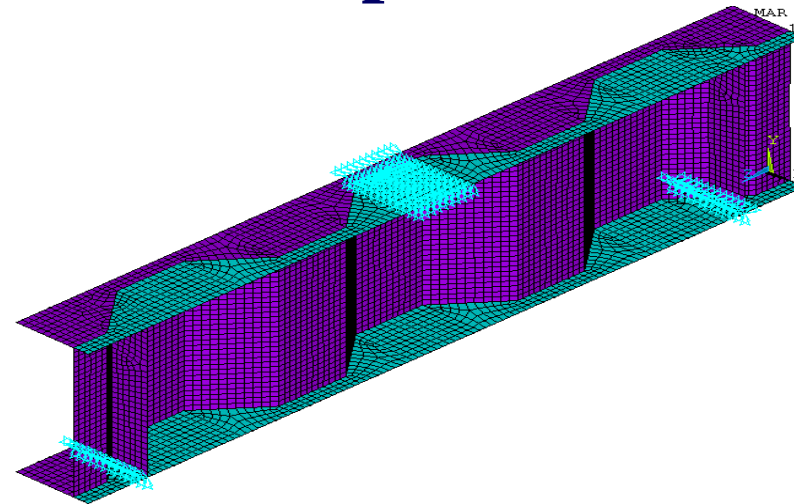
6. Recommendations for equivalent geometric imperfection

Aim: determination of the design value of the patch loading resistance by numerical simulation

Problem to be solved: \longrightarrow imperfection shape
 \longrightarrow imperfection scaling factor

Numerical model development

Finite element model



Experimental and numerical resistances

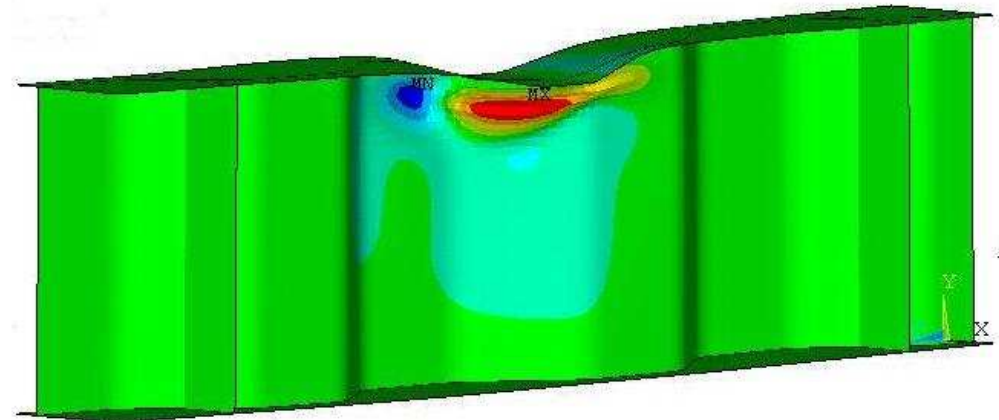
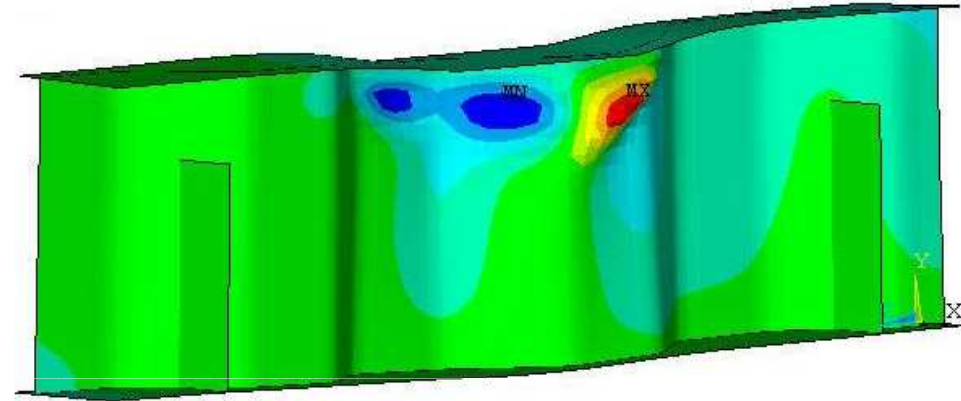
| | R_{exp} [kN] | R_{num} [kN] | difference [%] |
|--------------|----------------|----------------|----------------|
| 1. specimen | 754,20 | 771,08 | 2,2 |
| 2. specimen | 956,48 | 1044,18 | 9,2 |
| 3. specimen | 764,75 | 769 | 0,6 |
| 4. specimen | 949,02 | 969,054 | 2,1 |
| 5. specimen | 1192,01 | 1201,24 | 0,8 |
| 6. specimen | 1119,33 | 1155,901 | 3,3 |
| 7. specimen | 1077,72 | 1093,58 | 1,5 |
| 8. specimen | 1263,94 | 1285,4 | 1,7 |
| 9. specimen | 1220,48 | 1250,34 | 2,4 |
| 10. specimen | 1090,00 | 1120,4 | 2,8 |
| 11. specimen | 1280,99 | 1314,078 | 2,6 |
| 12. specimen | 772,39 | 781,05 | 1,1 |

Numerical model verification

experimental failure mode



numerical simulation

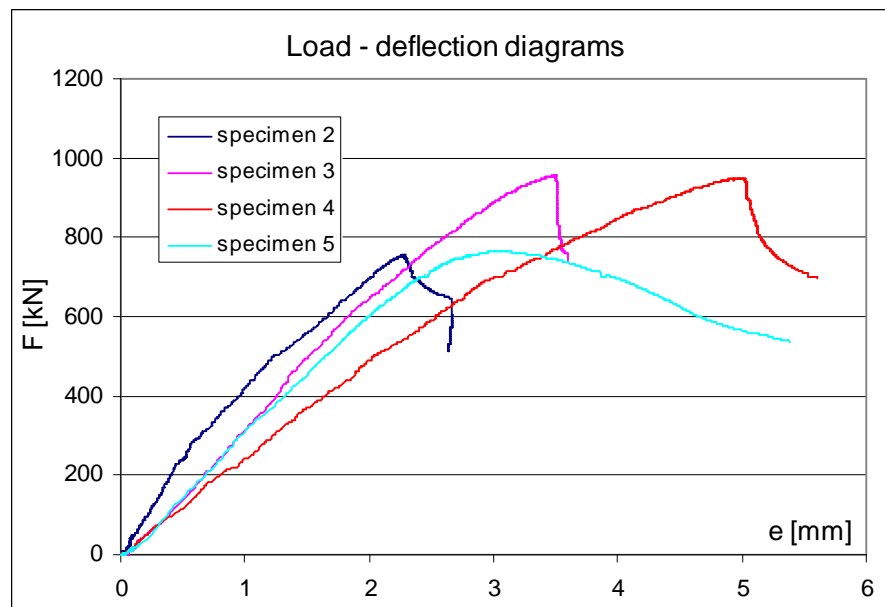




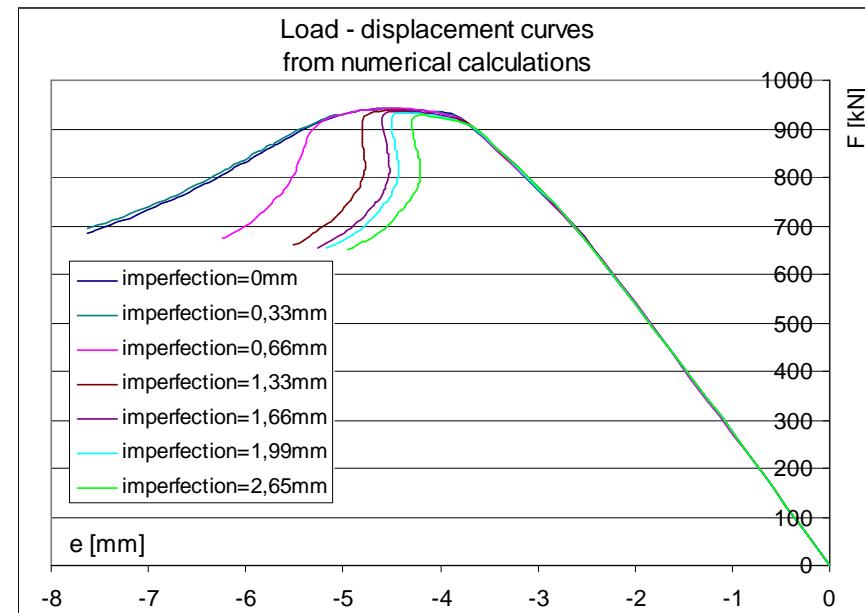
Numerical model verification

Observations in the experiments: different post-ultimate behaviours

Experimental load-displacement curves

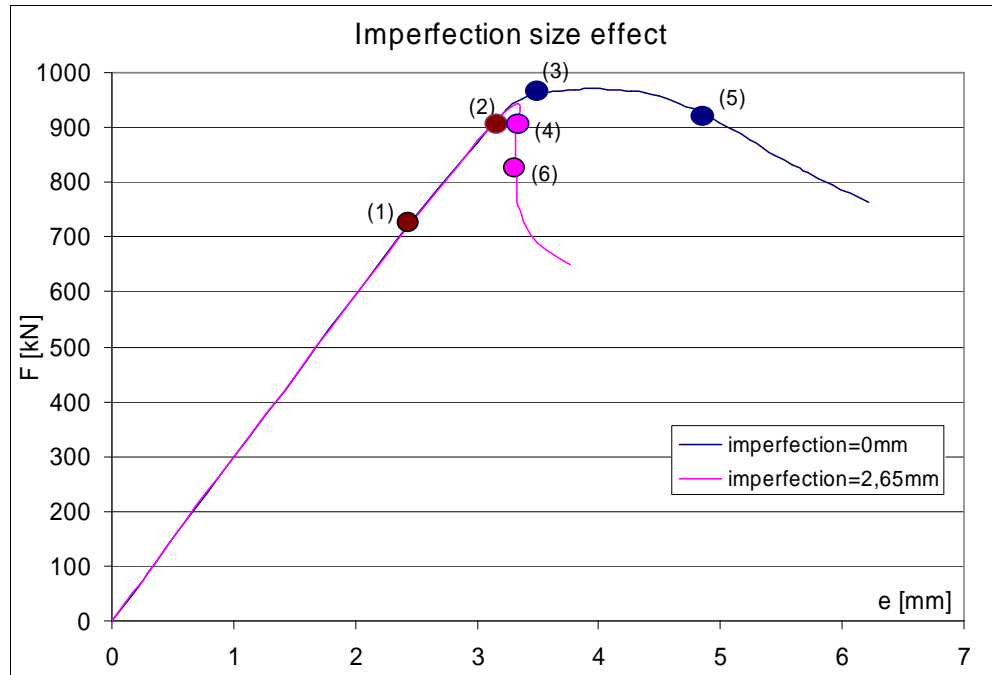


Numerical load-displacement curves



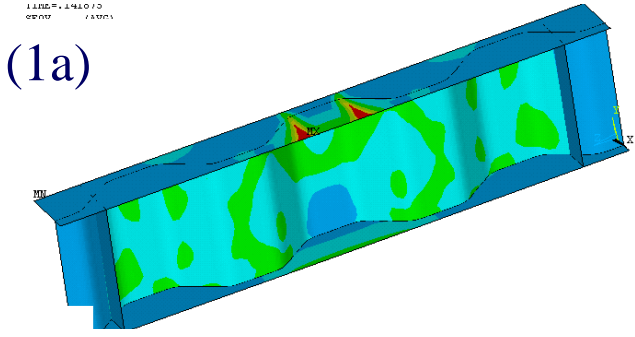
imperfections

Numerical model verification

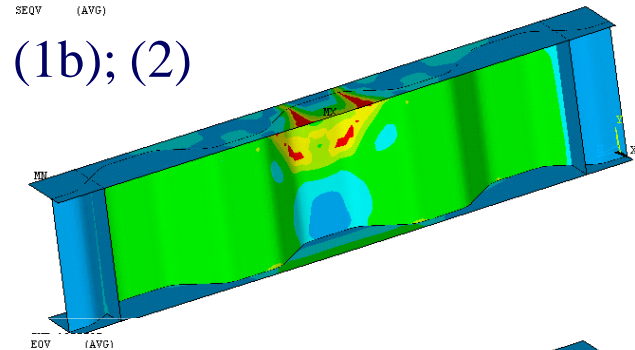


- (1) a, First yielding in the flange (imp. = 0mm)
- b, Yielding in the flange and web (imp. = 2,65mm)
- (2) First yielding in the web (imp. = 0mm)
- (3) - (4) 2 plastic hinges in the flange
- (5) - (6) 4 plastic hinges in the flange

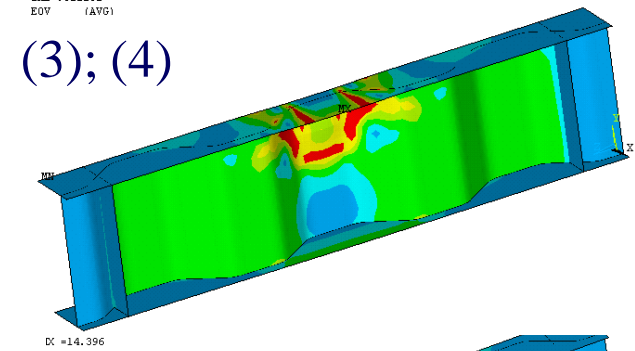
(1a)



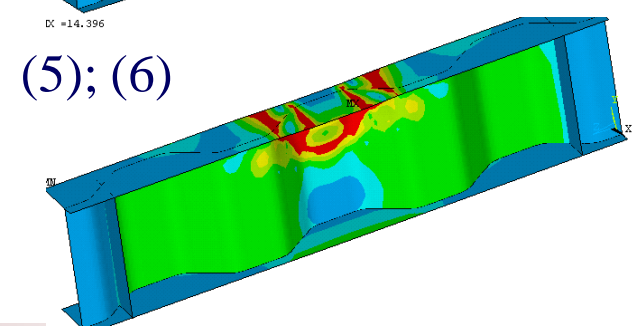
(1b); (2)



(3); (4)



(5); (6)

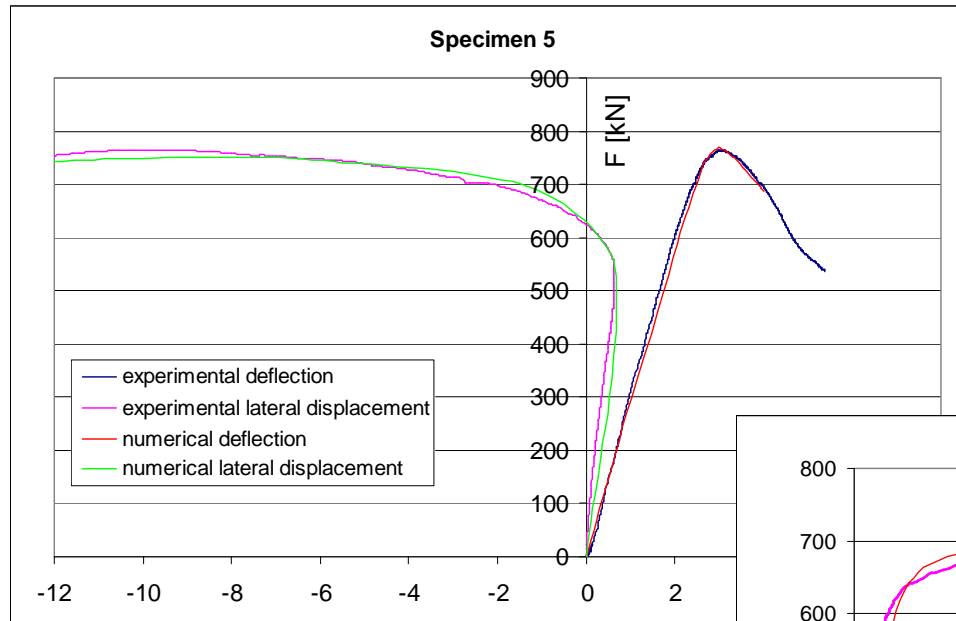


Numerical model verification

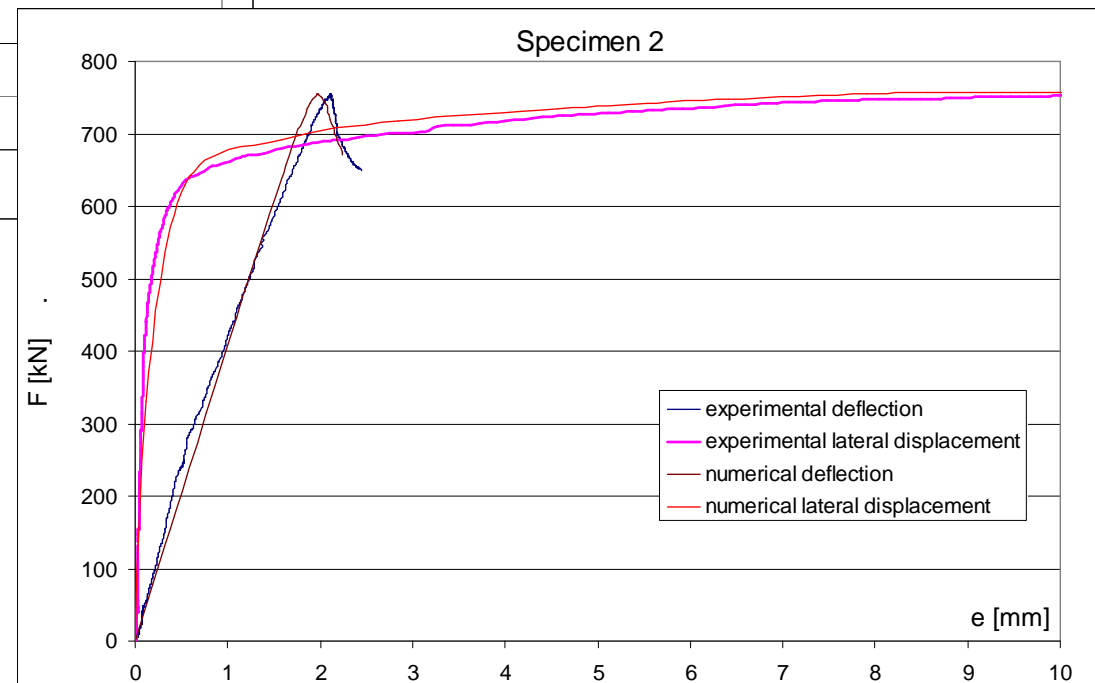
experimental load displacement diagram



numerical model



measured: - deflection
- lateral displacement
- applied force



FEM based design method

No recommendations for imperfection of corrugated webs in EC3-1-5



Possible standardised imperfection types



Aims

Based on executed experiments the development of recommendations for equivalent geometric imperfections.

shape

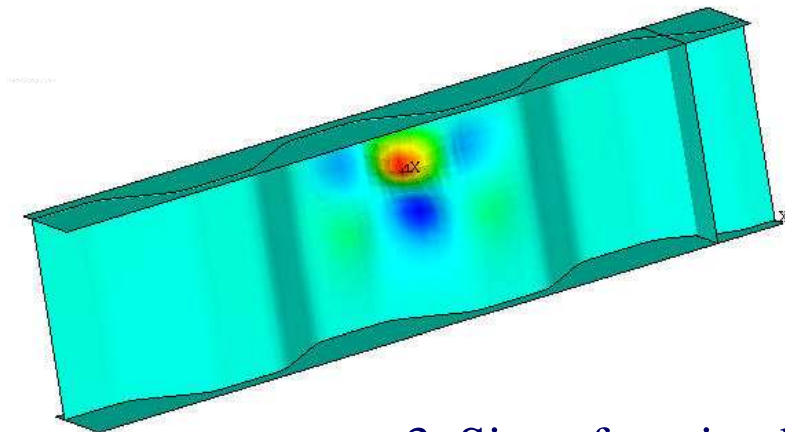
scaling factor

| Type of imperfection | Component |
|---|-----------|
| global member with length ℓ | |
| global longitudinal stiffener with length a | |
| local panel or subpanel | |
| local stiffener or flange subject to twist | |

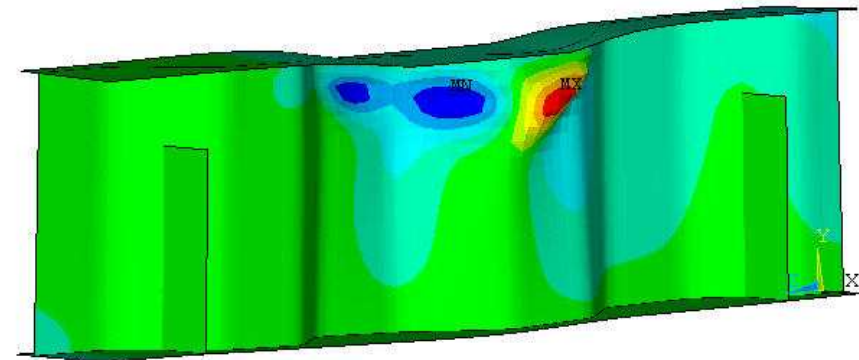
Figure C.1: Modelling of equivalent geometric imperfections

Equivalent geometric imperfection shape

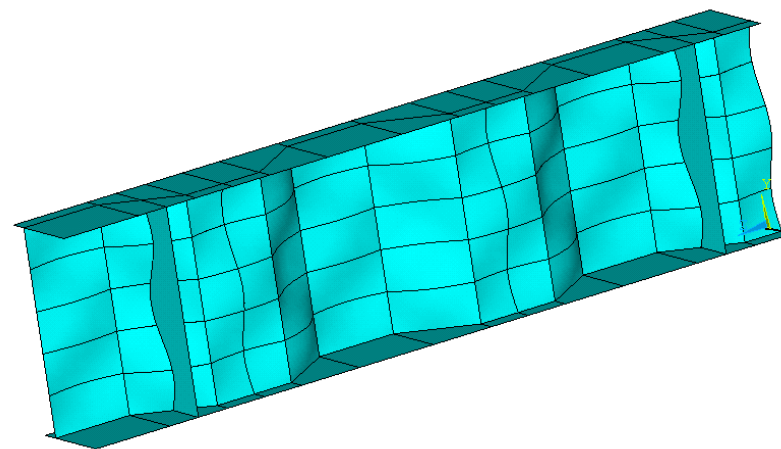
1. buckling mode



2. ultimate shape



3. Sinus function based on EC3 subpanel

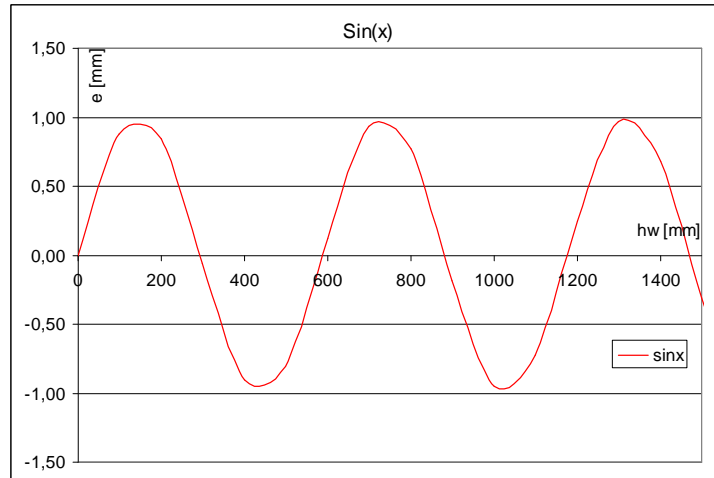




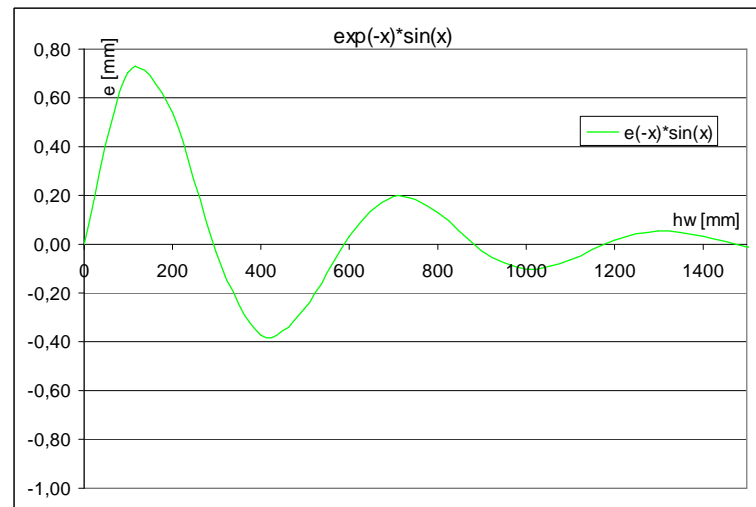
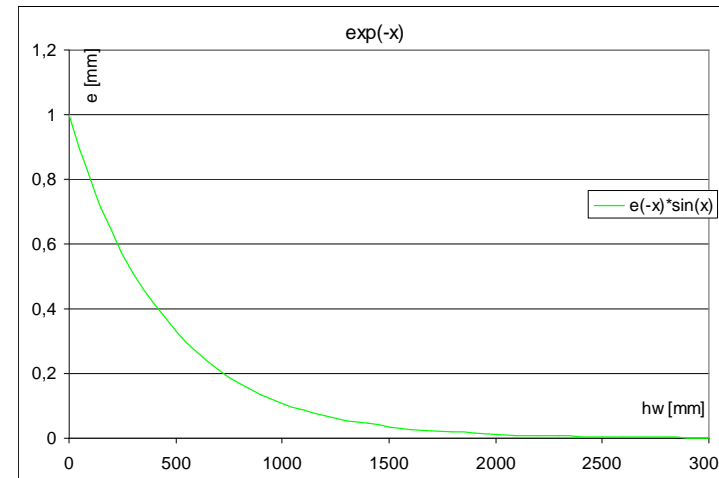
Equivalent geometric imperfection shape

4. numerical approach of the buckling mode:

$$f(x) = e^{-\frac{1}{Lm}x} \cdot \sin\left(\frac{1}{L} \cdot k \cdot \pi \cdot x\right)$$



X



k: distance between null points

m: falloff rate

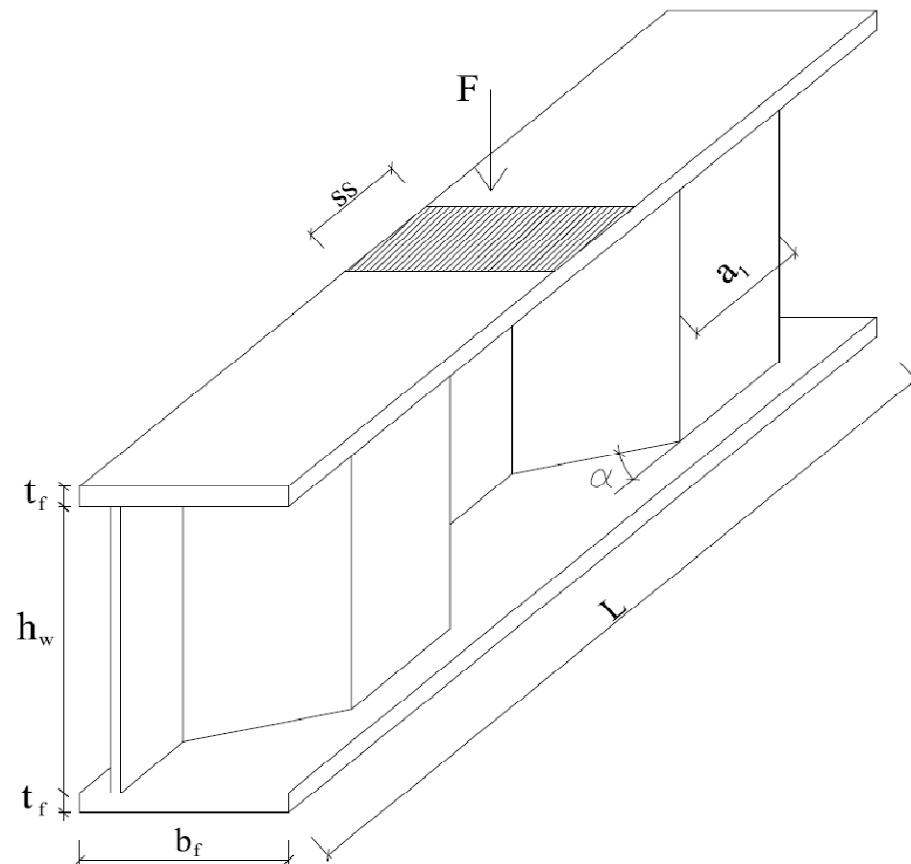
Equivalent geometric imperfection shape

Parameter study \longrightarrow influence of geometric parameters on the m and k

| parameters | m | k |
|------------|-----|-----|
| h_w | yes | yes |
| t_w | no | no |
| b_f | no | no |
| t_f | no | no |
| L | no | no |
| a_i | yes | yes |
| a | no | no |
| ss | yes | yes |

$$k = f(h_w/a_i, ss/a_i)$$

$$m = f(h_w/a_i, ss)$$



Equivalent geometric imperfection magnitude

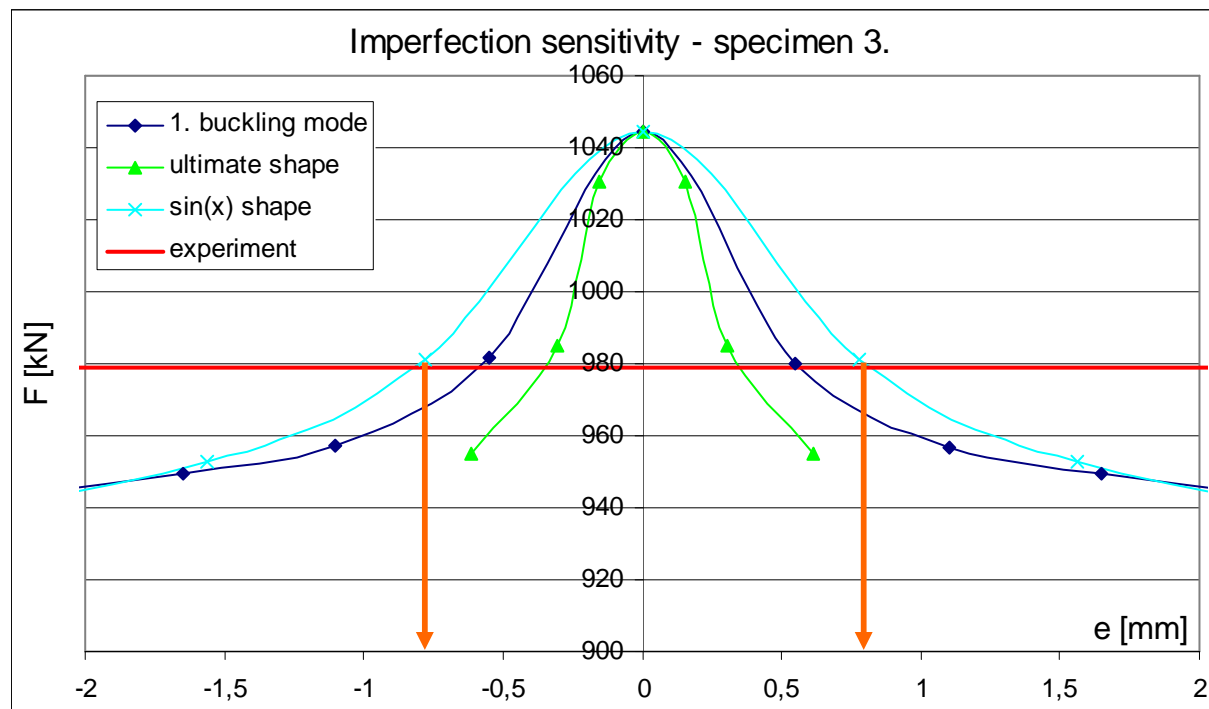
Scaling factor determination for:

1. first buckling mode
2. ultimate shape
3. sin(x) wave shape

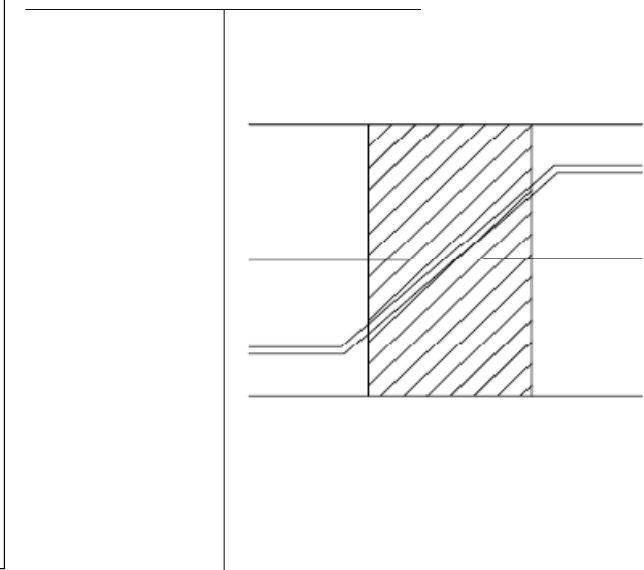
Experimental background:



Imperfection sensitivity for all three imperfection shapes.

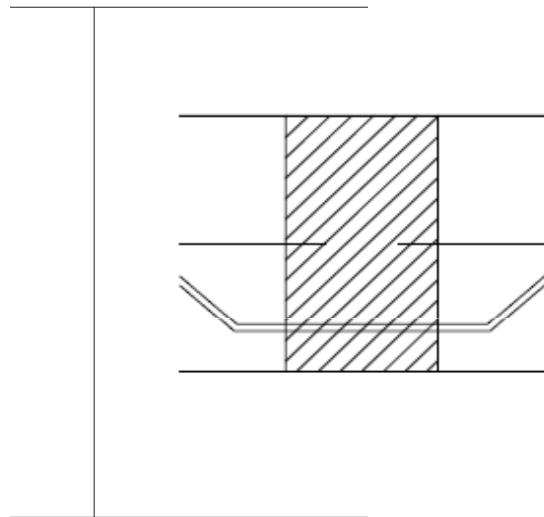
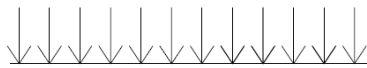


loaded fold: inclined

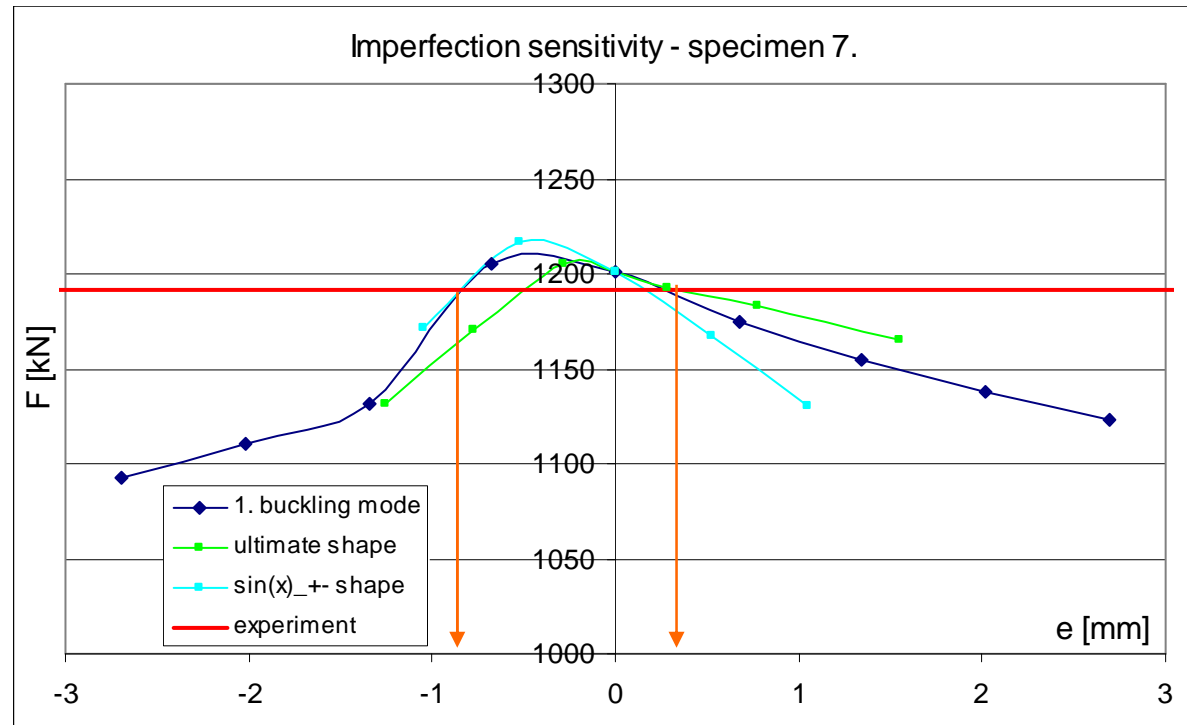


Equivalent geometric imperfection magnitude

loaded fold: parallel

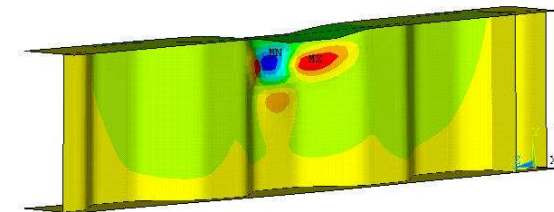
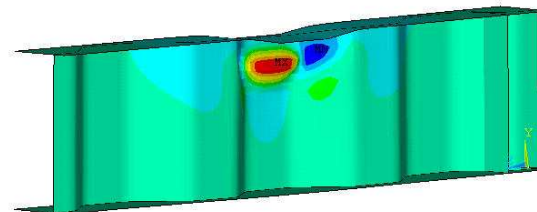


asymmetrical behaviour



negative value

positive value



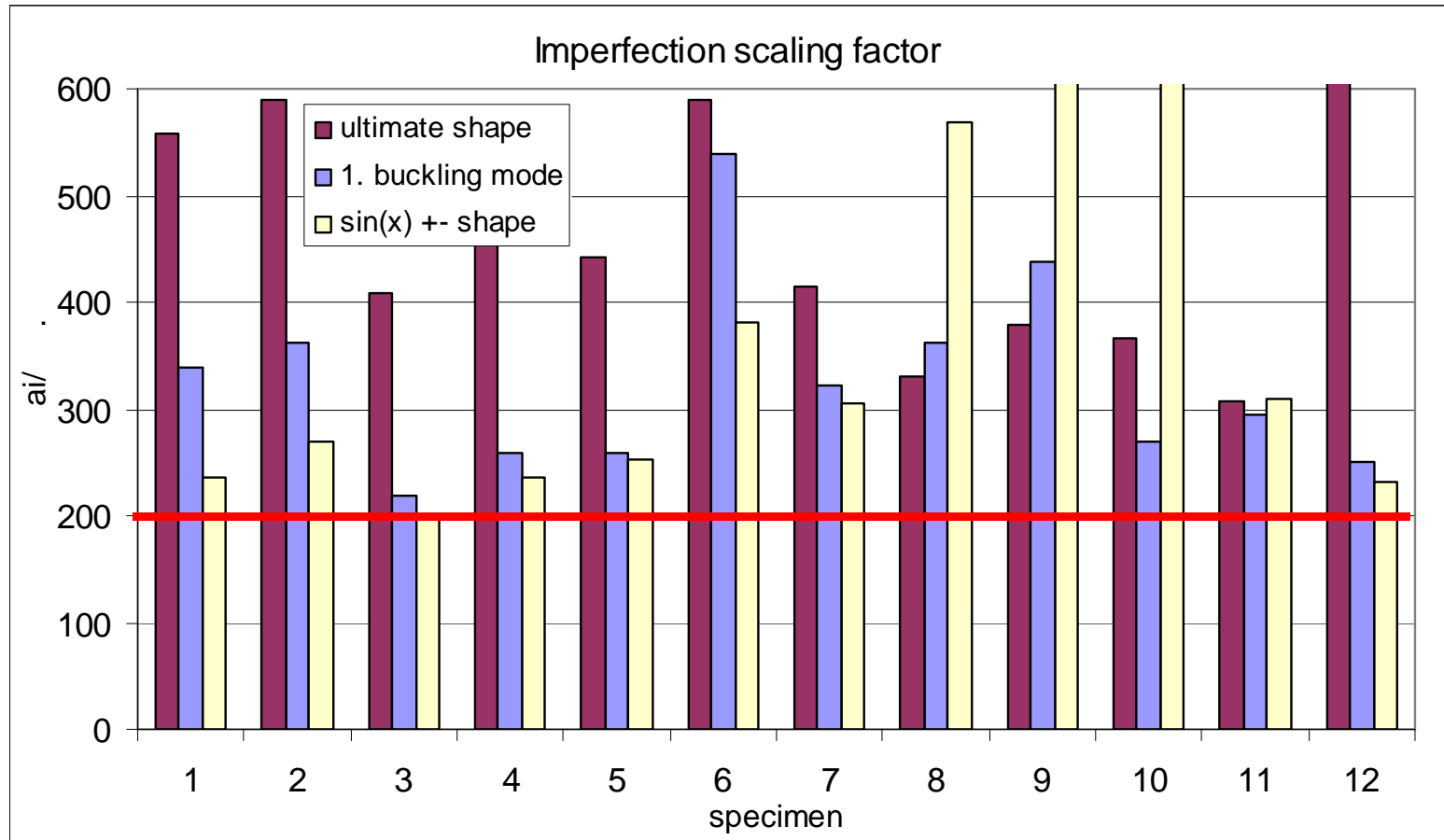
Compared to all tests results



imperfection scaling factors



Equivalent geometric imperfection magnitude



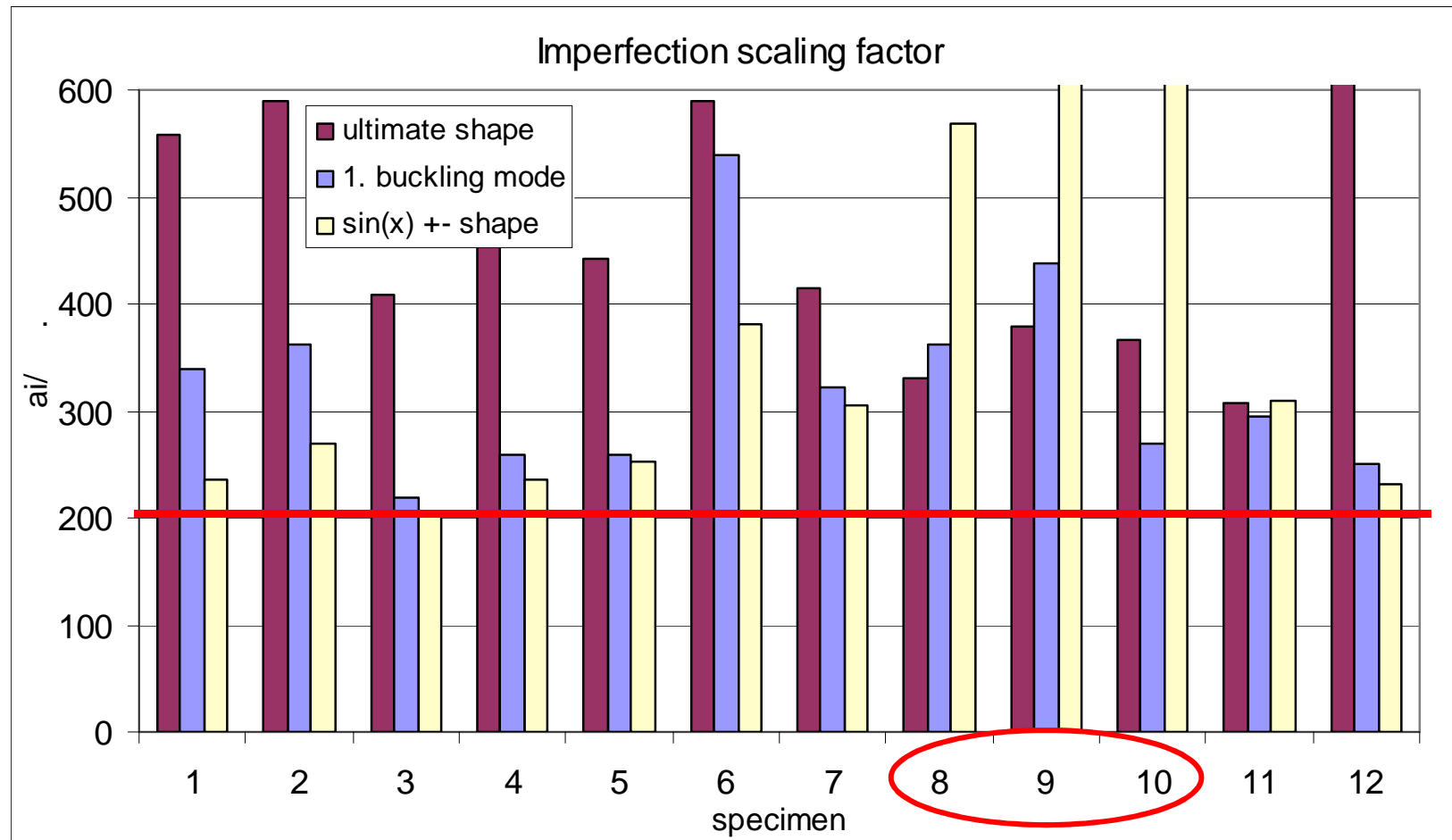
Imperfection scaling factor recommendations:

sin(x) shape imperfection: $a_i/200$

local buckling mode imperfection: $a_i/200$



Equivalent geometric imperfection magnitude

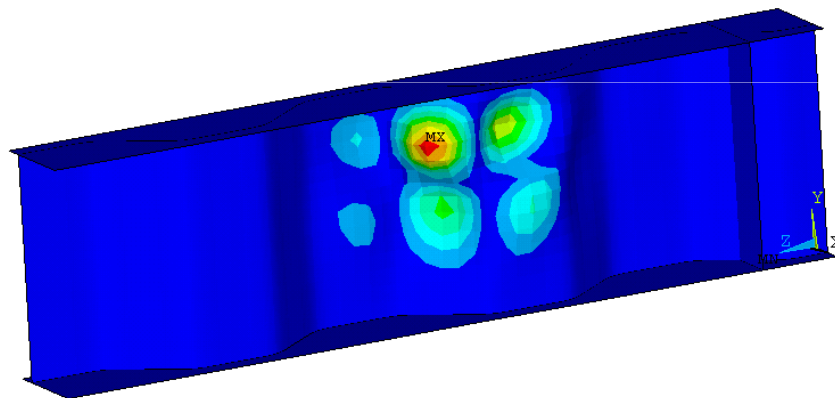


contradictions

Evaluation of ultimate shape imperfection

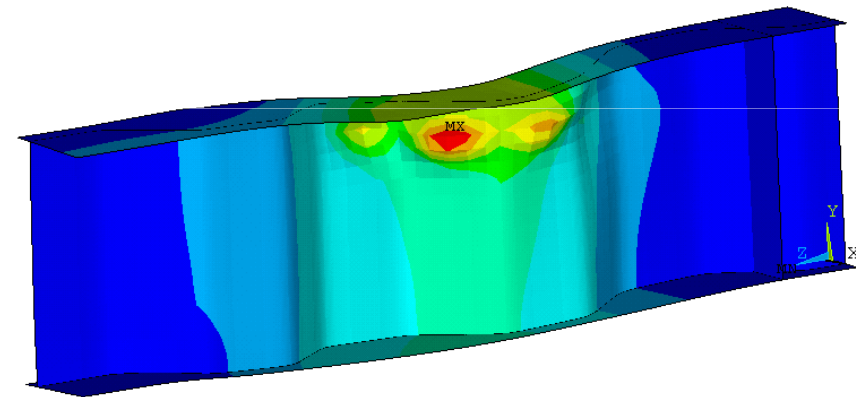
Unexpected cases: ultimate shape imperfection gives the largest resistance

First buckling mode



Imperfection in more waves

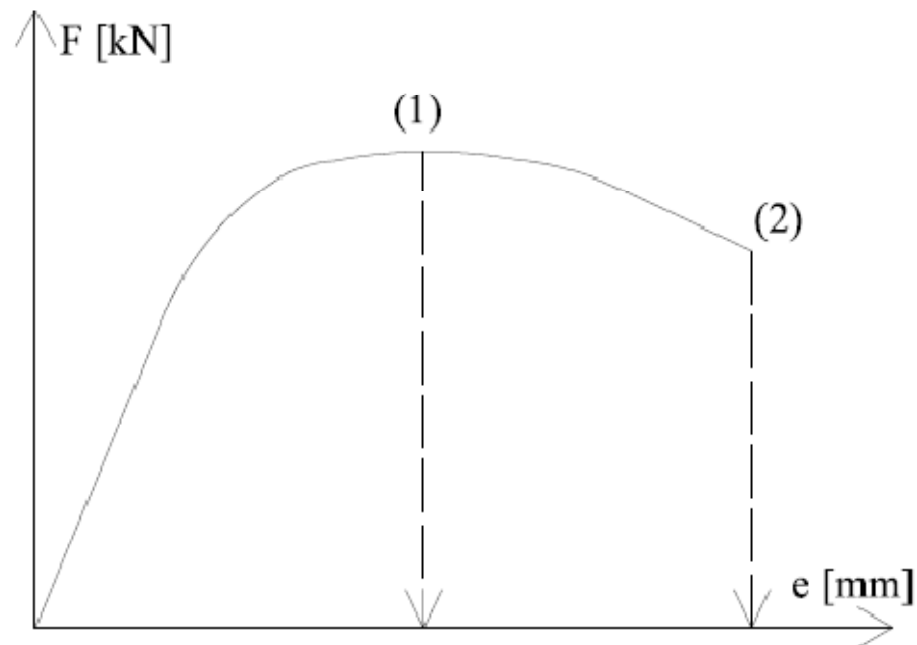
Ultimate shape



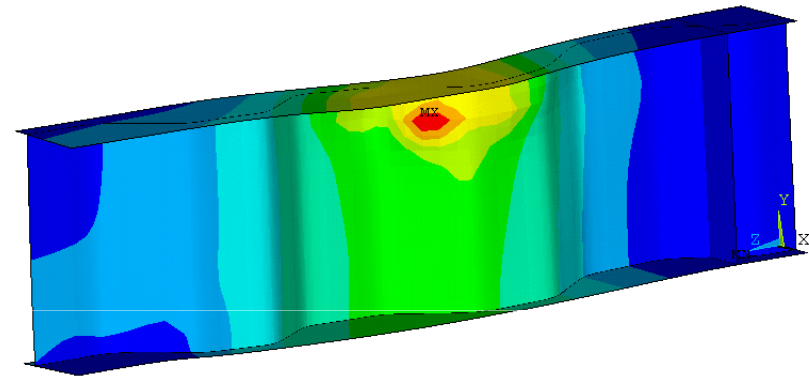
Imperfection only in 1 wave

Evaluation of ultimate shape imperfection

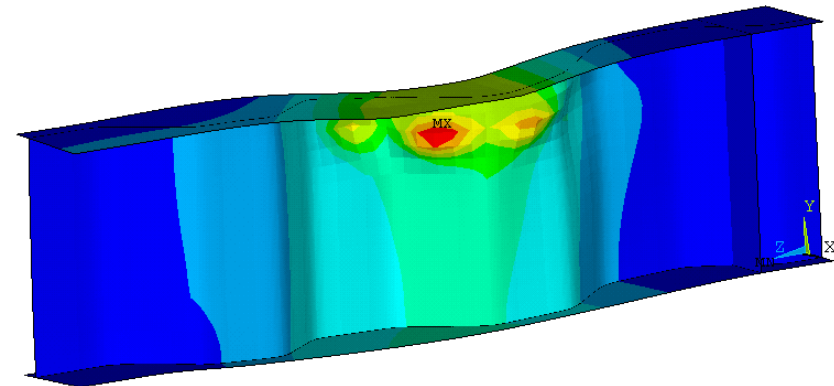
Ultimate shape in different
load steps:



Shape by point (1):



Shape by point (2):





Conclusions

Test results (12 large scale test specimens)



Numerical model development and verification



three investigated imperfections shapes + buckling shape prediction



Imperfection sensitivity analysis for different imperfection shapes



Imperfection shape and scaling factor determination



Proposal for FEM based design method



Thank you for your attention!